Breaking Mifare DESFire MF3ICD40: Power Analysis and Templates in the Real World — Extended Version*

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Abstract. With the advent of side-channel analysis, implementations of mathematically secure ciphers face a new threat: by exploiting the physical characteristics of a device, adversaries are able to break algorithms such as AES or Triple-DES (3DES), for which no efficient analytical or brute-force attacks exist. In this paper, we demonstrate practical, non-invasive side-channel attacks on the Mifare DESFire MF3ICD40 contactless smartcard, a 3DES-based alternative to the cryptanalytically weak Mifare Classic [9, 25]. We detail how to recover the complete 112-bit secret key of the employed 3DES algorithm, using non-invasive power analysis and template attacks. Our methods can be put into practice at a low cost with standard equipment, thus posing a severe threat to many real-world applications that employ the DESFire MF3ICD40 smartcard.

Keywords: contactless smartcard, side-channel analysis, templates, DESFire

1 Introduction

Radio Frequency Identification (RFID) technology has become the basis for numerous large-scale, security-relevant applications, including public transport, wireless payment, access control, or digital identification [39]. The information stored on RFID smartcards, e.g., personal data, or cash balance, is often highly sensitive — however, the access to the air interface and to the device itself is virtually impossible to control. Hence, most modern RFIDs feature cryptographic mechanisms, including encryption and authentication, in order to thwart attacks such as eavesdropping, manipulation, or cloning of a smartcard.

Mifare DESFire MF3ICD40 is a contactless smartcard featuring a cryptographic engine for authentication and encryption based on (Triple-)DES. The smartcard is employed in several large payment and public transport systems around the world, e.g., the Czech railway in-karta [7], the Australian myki

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card [36], or the Clippercard used in San Francisco [40]. In the course of our research, we also noticed many smaller installations, e.g., for mobile payment or access control, that are based on the Mifare DESFire MF3ICD40. From a mathematical point of view, the employed 3DES cipher is secure, because no efficient cryptanalytical attacks are known. Thus, in this paper, we focus on side-channel attacks, i.e., methods that target the physical implementation of the cryptographic primitive in soft- or hardware. Using non-invasive and hence non-detectable measurement of the electro-magnetic (EM) emissions of the device, we are able to completely recover the secret 112-bit master key and thus to, for example, read out, manipulate, or duplicate the contents of a Mifare DESFire MF3ICD40 card.

1.1 Related Work

The idea of exploiting physical side-channels to attack hardware implementations of secure ciphers was first put forward in [20] in 1998. Since then, a lot of research has been conducted in this area, with important contributions including the analysis using the EM emanation of a device [1] or the application of the correlation coefficient in Correlation Power Analysis (CPA) to better model the physical behaviour of Integrated Circuits (ICs) [2]. At CHES 2002, the authors of [5] proposed the use of machine learning techniques such as pattern recognition for Side-Channel Analysis (SCA) and coined the notion of “template attacks”. Several extensions and improvements for this approach have been suggested in the last few years, cf. [31, 33, 35].

The susceptibility of ciphers running on RFID devices towards SCA was initially shown in [12, 30]: the authors present attacks on a white-box software implementation of the AES executed by a standard, unprotected microcontroller (μC) on a self-made prototype RFID, evaluating techniques to overcome problems such as misalignment of the measured signals.

With respect to the application of SCA to break commercial, real-world devices, few papers have been published, as most research in this field is carried out by evaluation labs behind closed doors. The potential impact of SCA in practice was demonstrated by the complete break of the proprietary KeeLog system presented at CRYPTO 2008 [8]. Results for the black-box analysis of a contactless smartcard are given in [17], proposing a leakage model for RFIDs that forms the basis for our analyses and is outlined in Sect. 2. However, the authors are unable to recover the complete key and do not disclose to which device their attacks apply. In [18], the application of analog demodulation for SCA of RFIDs is presented for the first time. The measurement setup used in the present paper is an extension of the setup described in [18].

1.2 Contribution of this Paper

The work presented in this paper is of practical nature: we highlight the relevance of SCA in the real-world by demonstrating the first full key-recovery attack on the popular Mifare DESFire MF3ICD40 smartcard reported in the literature.
Doing so, we point out problems and obstacles that occur when conducting SCA in practice which are often neglected in academic papers. In addition, we present the — to our knowledge — first application of template attacks to break cryptographic RFID devices, allowing for potentially very fast determination of the secret key. The remainder of this paper is structured as follows: In Sect. 2, we give the signal-theoretical background of our measurement setup for RFID devices, which is presented in Sect. 3. We then practically apply the developed techniques to analyze the smartcard in Sect. 4, detailing on the internal hardware structure of the device. In Sect. 5, we extend our findings and present a successful full key-recovery attack on the 3DES engine. After that, in Sect. 6, we demonstrate a different approach for obtaining the secret key based on template attacks to eavesdrop on the internal database. Finally, we conclude in Sect. 7, discussing the implications of our findings for commercial applications and giving directions for further research.

2 Demodulation for SCA of Contactless Smartcards

For contactless smartcards, the energy for operation is supplied wirelessly using magnetic coupling. As proposed in [17, 18], this gives rise to a different leakage mechanism compared to contact-based devices. In a similar manner as for regular data transmission, the 13.56 MHz field generated by the reader is load-modulated by the power consumption of an RFID\(^1\).

Let the power consumption of the target device be given as \( p(t) = P_{\text{const}} + p_{\text{dyn}}(t) \), where \( P_{\text{const}} \) is the constant part and \( p_{\text{dyn}}(t) \) the fraction caused by internal operations, e.g., intermediate values being manipulated during a cryptographic operation. Usually, the dynamic portion of the power consumption is far weaker than the constant part, i.e., \( |p_{\text{dyn}}(t)| \ll P_{\text{const}} \). The leakage exploitable for an SCA thus heavily depends on the quality of the isolation and amplification of \( p_{\text{dyn}}(t) \). As mentioned, in an RFID setting, the amplitude of the reader signal is modulated by \( p(t) \), i.e., \( s(t) = p(t) \cdot \cos(\omega_r \cdot t) \cdot (P_{\text{const}} + p_{\text{dyn}}(t)) \cdot \cos(\omega_r \cdot t) \).

where \( \omega_r = 2\pi f_r \), \( f_r = 13.56 \text{ MHz} \) is the standard carrier frequency. Clearly, the extraction of \( p(t) \) (and especially of the weak dynamic portion) from \( s(t) \) can be done using amplitude demodulation, cf. for instance [34]. In practice, “incoherent” techniques (i.e., for which a separate, unmodulated carrier signal is not necessary) based on rectification (often called envelope detection) are very common, and in this paper, we follow that approach as well. The principle due to which rectification can be used for demodulation is best understood in the frequency domain, following [27]. First note that, as stated above, \( |p_{\text{dyn}}(t)| \ll P_{\text{const}} \) and hence, \( |s(t)| = |P_{\text{const}} + p_{\text{dyn}}(t)| \cdot |\cos(\omega_r \cdot t)| = (P_{\text{const}} + p_{\text{dyn}}(t)) \cdot |\cos(\omega_r \cdot t)| \).

Let \( P(j\omega) = \text{DFT} \{ p(t) \} = \text{DFT} \{ P_{\text{const}} + p_{\text{dyn}}(t) \} \) denote the frequency-domain representation of the signal that is to be reconstructed. By expanding

\(^1\) however, for data transmission, the fluctuations of the EM field are intentional and far stronger in magnitude
\[ |\cos(\omega_r \cdot t)| \] using its Fourier series, one obtains the spectrum of the rectified signal:

\[
\text{DFT} \{ |s(t)| \} = \text{DFT} \{ p(t) \cdot |\cos(\omega_r \cdot t)| \} = \frac{2}{\pi} \sum_{\nu=-\infty}^{\infty} \left( \frac{(-1)^\nu}{1 - 4\pi^2} \right) e^{j2\nu\omega_r t}
\]

\[
= \frac{2}{\pi} \sum_{\nu=-\infty}^{\infty} \left( \frac{(-1)^\nu}{1 - 4\pi^2} \right) \text{DFT} \{ p(t) \cdot e^{j2\nu\omega_r t} \} = \frac{2}{\pi} \sum_{\nu=-\infty}^{\infty} \left( \frac{(-1)^\nu}{1 - 4\pi^2} \right) P(j\omega - j2\nu\omega_r)
\]

The rectified signal is essentially formed by the spectrum of \( P_{\text{const}} + P_{\text{dyn}}(t) \), which, however, is (scaled and) repeated at all even multiples of the carrier frequency \( \omega_r = 2\pi \times 13.56 \text{MHz} \). Thus, the first repetition occurs at 27.12 MHz. Using a low-pass filter with a cutoff frequency less than 13.56 MHz isolates the desired signal\(^2\) \( p(t) \).

### 3 Measurement Setup

For the analysis of the DESFire MF31CD40, we extended the measurement environment of [18]. Fig. 1a gives an overview over the components of our setup. A custom, freely programmable RFID reader [16] compliant to ISO 14443 [13, 14] and ISO 15693 [15] supplies the contactless smartcard (from now on occasionally referred to as Device Under Test (DUT)) with power and handles the communication, for instance to trigger an encryption operation.

A wide-band EM probe with a suitable pre-amplifier [21] captures the magnetic near-field in the proximity of the IC, resulting in a “raw” signal (denoted as (2) in Fig. 1a) which is dominated by the 13.56 MHz carrier frequency of the reader. On the one hand, this signal is directly recorded and stored using a Picoscope 5204 Digital Storage Oscilloscope (DSO) [29] at a sample rate of 500 MHz; on the other hand, it is passed to an analog demodulator that performs the operations outlined in Sect. 2 to facilitate SCA, resulting in the signal (1) in Fig. 1a. The central PC controls the measurement process, i.e., prepares and sends commands to the DUT via the RFID reader and acquires and stores the resulting side-channel signals (1) and (2) (from now on referred to as \( \text{braces} \)).

As explained in Sect. 2, analog demodulation is required to separate the actual power consumption signal from the carrier signal and to thereby improve the quality of the (exploitable) side-channel leakage. Accordingly, we developed a custom Printed Circuit Board (PCB) comprising a full-wave rectifier and appropriate filter circuitry to perform the incoherent demodulation approach. Fig. 1b shows the basic structure of the demodulation circuitry. The full schematics are given in an appendix in the extended version of this paper [28]. The full-wave rectifier is formed by two isolated half-wave rectifiers, each employing an BAT43 Schottky diode [38]. To rectify the negative part of the input (1), the signal is first inverted and then rectified by the diode, yielding signal (3) in Fig. 1b. For the positive portion, the buffer amplifier only provides isolation of the input signal and driving of the corresponding diode, but does not perform inversion to

\(^2\) the constant term \( P_{\text{const}} \) can be removed with a highpass filter that only blocks the DC and very low-frequency components.
produce signal 2. The two resulting parts 2 and 3 are then added to form the full-wave rectified output 4.

A third-order LC bandpass filter extracts the baseband part, i.e., the portion of the spectrum centered around 0 Hz. In our case, the −3dB frequency was specified to 12 MHz. Additionally, the filter also suppresses frequency components below 10 kHz to remove the constant part of the modulating signal. Finally, the output amplifier adjusts the amplitude of the signal in order to optimally utilize the minimum input range of ±100 mV of the Picoscope and drives a 50 Ω load, i.e., a suitable coaxial cable.

In the case that a raw signal (i.e., 2 in Fig. 1a) is used for SCA, it was shown in [17] that the demodulation has to be performed digitally in order to conduct a successful CPA, i.e., digital pre-processing is mandatory. For the output of the analog demodulator, digitally filtering the output signal 1 is optional, however, might help to further reduce the 13.56 MHz frequency component still present due to certain characteristics of the analog circuits. For a more detailed description of the effects of the respective processing techniques, cf. [18].

In order to illustrate the effect of the analog and digital processing in summary, Fig. 2 shows the power spectra\(^3\) of signals 1 (Fig. 2a) and 2 (Fig. 2b) before and after digital processing, respectively.

4 Practical Results: Profiling of Mifare DESFire MF3ICD40

Mifare DESFire MF3ICD40 [26] is a contactless smartcard initially designed by the semiconductor division of Philips, which became the separate company NXP in 2006. The card is compliant to parts 1-4 of the ISO 14443A standard. A communication with the card can be performed in plain, with an appended Message Authentication Code (MAC), or with full data encryption using 3DES. The device offers 4 kByte of storage that can be assigned to up to 28 different applications, whereas each application may hold a maximum of 16 files. Depending on the configuration of the access rights, a mutual authentication protocol has

\(^3\) i.e., the squared magnitude |DFT \{s(t)\}|\(^2\) of the Discrete Fourier Transform (DFT)
to be carried out before accessing the card, ensuring that the symmetric 3DES keys of the card $k_C$ and of the reader $k_R$ are identical.

According to specifications found on the internet, the smartcard features several functions to thwart physical attacks such as SCA, fault injection, or reverse-engineering; the IC is built using asynchronous circuits and employs a custom, asynchronous μC design based on the 8051 architectures. Besides, all digital units (i.e., control logic, cryptographic engine etc.) are “intermingled” so that no functional block are discernible, a technology called “glue logic” by the vendor. Note that all results in this paper do not directly apply to the newer AES-based variant DESFire EV1. The authentication protocol of the DESFire

$$\text{Reader} \quad \text{DESFire MF3I CD40}$$

\[
\begin{align*}
\text{begin} & \quad \text{Generate } n_c \in \{0, 1\}^{64} \quad \{\text{Step 1}\} \\
B_0 & \quad 3\text{DES}_{k_C}(n_c) \\
\text{Choose } B_1, B_2 & \quad C_2 = 3\text{DES}_{k_C}(B_2) \\
 & \quad C_1 = 3\text{DES}_{k_C}(B_1) \quad \{\text{Step 2}\}
\end{align*}
\]

Fig. 3: Excerpt of the Mifare DESFire authentication protocol relevant for SCA

MF3I CD40 has been disclosed and can for instance be found in [19, 4]. For the purpose of SCA, we refer to a simplified version in the following, given in Fig. 3. $k_C = (k_{C,1}, k_{C,2})$ is the 128-bit 3DES master key (including the parity bits) used by the DUT, whereas the two halves are of size 64 bit each, i.e., $k_{C,1}, k_{C,2} \in \{0, 1\}^{64}$. $3\text{DES}_{k_C}(x) = \text{DES}_{k_{C,1}}\left(\text{DES}_{k_{C,2}}^{-1}\left(\text{DES}_{k_{C,1}}(x)\right)\right)$ denotes a 3DES encryption of a 64-bit value $x$ in Encrypt-Decrypt-Encrypt (EDE) mode.
The full command set\(^4\) has been implemented for our custom reader mentioned in Sect. 3.

Initially, we are facing a black-box scenario, i.e., have (apart from the command set and the specifications in the datasheet) no further knowledge on the inner workings of the device. Hence, profiling to map different portions of a power trace to steps of the operation of the DUT (e.g., a data transfer or an encryption operation) is mandatory before attempting to perform real attacks on cryptographic operations. As a first step, we dismantled the IC, took magnified photographs of the silicon die, cf. Fig. 4a, and tried to distinguish the different parts of the circuit. The hypothetical structure depicted in Fig. 4b is a result of this optical inspection and the findings reported in the remainder of this section.

![IC photo and hypothetical structure](image)

**Fig. 4:** The DESFire MF3IC40 IC

To prepare the actual SCA, we recorded side-channel traces for both steps of the authentication protocol, separately varying either the key of the card \(k_C\) or the values for \(B_1\) and \(B_2\) in step 2. To estimate the effect of our analog processing circuitry, we both store the “raw” signals before demodulation (\(^2\) in Fig. 1a) and the result of the demodulation process (\(^1\) in Fig. 1a).

We then perform several CPAs to locate the points in time in the power traces at which the known values for \(k_C\), \(B_1\) and \(B_2\) (and the encryption results \(C_1\), \(C_2\)) are processed. Employing an 8-bit Hamming weight model, all mentioned values can be precisely pinpointed, cf. Fig. 5. We observed a stable value of \(\approx 0.15\) for the respective correlation coefficient after around 1,000 traces. This suggests that internally, an 8-bit data bus is used to connect the \(\mu C\) to the memory and the cryptographic engine, yielding the structure of Fig. 4b. For each byte transferred over this bus, a distinct peak appears in the power trace,

\(^4\) including the necessary commands for changing the key, performing a full authentication etc.

\(^5\) as we know \(k_C\) during the profiling phase, we can predict these values that are never output by the DUT
whereas the distance between two such peaks indicates an internal bus frequency of $f_{bus} \approx 282.5$ kHz $= 13.56/48$ MHz. Note that the peaks for data bus transfers later in a trace, e.g. for $B_2$ or $C_2$ in Fig. 5b, are often misaligned, i.e., their exact position slightly varies from execution to execution. The reason for this behaviour lies in the non-constant execution time of a 3DES operation, which is further detailed in Sect. 5. Hence, it is necessary to re-align the respective parts (for instance, using standard pattern matching approaches [23]) to obtain a significant correlation.

5 Practical Attack: CPA of the 3DES engine

Having located the input and output values of the 3DES encryption, we now focus on this part to perform the recovery of the secret key. Fig. 6 depicts the part of the trace assumed to represent the first (Single-)DES encryption of $3DES_{k_3} (B_2)$ (Fig 6a) and the associated frequency spectrum (Fig. 6b, with (blue, solid) and without (green, dashed) the analog rectifier).

Comparing this part for several traces, we notice some interesting properties: first, the length of one DES operation varies from execution to execution, even if the input data and the key are kept constant. This hints at a countermeasure based on randomization in time being employed to thwart CPA. We further address this problem in Sect. 5.1. Second, the amplitude of the traces is significantly lower during the supposed encryption, which coincides with the statements in the available DESFire documentation that a dedicated low-power hardware engine performs the cryptographic operation.

To prepare the actual key-recovery, we first attempt to characterize the leakage of the 3DES engine and find a suitable power model by correlating with the full intermediate 64-bit states$^6$ using a known key. Conducting several experi-

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$^6$ i.e., $(L_i^{(n)}, R_i^{(n)})$, $0 \leq i \leq 16$, $n \in \{1, 2, 3\}$, where $n$ denotes the Single-DES iteration within the complete 3DES, for details cf. [24]
Fig. 6: First DES iteration of the 3DES encryption on the Mifare DESFire MF3ICD40

ments, we found the Hamming distance model to yield a significant correlation and were able to locate the first few rounds of the DES, as depicted in Fig. 7 for rounds 0→1, 5→6, 10→11, and 0→1 of the second DES iteration.

Fig. 7: Correlation coefficients for the Hamming distances between rounds of the 3DES, 500,000 traces

However, as evident from Fig. 7a, this approach only is able to locate the first few rounds (with decreasing correlation), supposedly due to the randomization mentioned above. Statistically analyzing the length of the first DES iteration using 100,000 traces, we observe that one iteration takes 8.2 μs on average. This duration varies in discrete steps of 290 μs over a total range from 6.9 μs to 9.1 μs. This suggests that the cryptographic engine executes up to eight \([([9.1 - 6.9]/0.29])\) “dummy” rounds based on an internal Random Number Generator (RNG) to impede SCA.

To solve this problem, we tried out methods to overcome misalignment suggested in the literature, including comb filtering or windowing [8], Dynamic Time Warping (DTW) [37], and Differential Frequency Analysis (DFA) [10, 30]. Our results show DFA to yield the best overall correlation, using the following steps:
before correlating with the prediction of the power model, a trace is partitioned into (overlapping) segments, these segments are transformed to the frequency domain with the DFT, and the phase information is discarded by taking the absolute value of the DFT coefficients. The optimal value for the size of each segment was determined to be 1.5 µs, with an overlap of 75% between adjacent segments. The strongest leakage occurs for low frequencies, hence, we limited the analysed spectral range to 0...16 MHz. Fig. 7b shows the according correlation coefficients for the respective rounds of the cipher — in contrast to the analysis in the time domain, all rounds are clearly distinguishable.

In order to quantify the improvement caused by the employed analog and digital processing methods, we compare the maximum correlation coefficient over the number of traces for the 32-bit Hamming distance $R_0 \rightarrow R_1$ (again, using a known key), with a detailed plot of the respective values given in an appendix in [28], with a detailed plot of the respective values given in Fig. 13 in Appendix B.

In all cases, the correlation converges rather quickly to a significant value far greater than $\sqrt{\text{No. of traces}}$, yet, a distinct gain due to both analog and digital processing is discernible: while the digitally demodulated traces without re-alignment by DFA result in a stable value of $\approx 0.015$, the combination of analog demodulation with DFA yields $\approx 0.032$, that is, an improvement by a factor of two. As a result, we utilize these pre-processing techniques for the full key-recovery presented in Sect. 5.1, taking the fact into account that in this case, we have to target each 4-bit S-Box output separately, so smaller overall correlations are to be expected.

### 5.1 Full Key-Recovery

Based on the findings of the profiling phase, a CPA can be mounted to obtain the full 3DES key by recovering the 6-bit part of the round key for each S-Box, starting with the first round of the first DES. To make use of all available information, a natural choice is to target the full 4-bit output of each S-Box in the Hamming distance $R_0 \rightarrow R_1$. However, for the case of the DESFire MF31CD40, this turned out to be problematic: Fig. 8 shows the maximum correlation coefficients for the correct key candidate for a standard CPA in the time domain and DFA in the frequency domain, respectively. Although the complete key is discernible after $\approx 450,000$ traces in Fig. 8a, the stable value for the correlation significantly differs depending on the S-Box, causing the attack to fail for five S-Boxes when performed without re-alignment by means of DFA, cf. Fig. 8a. Testing other prediction functions, a single-bit CPA (which is equivalent to the classic Differential Power Analysis (DPA)) proved to be the most successful approach. As depicted in Fig. 9, for each S-Box there is at least one bit providing sufficient leakage to allow our attack to succeed after approx. 250,000 traces and 350,000 traces with and without DFA, respectively.

For the sake of optical clarity, the maximum correlation for wrong key candidates has been omitted in the above figures. Yet, we performed the actual key-recovery computing these correlations as well and verified that in all cases,
the correlation for the wrong candidates is below \( \frac{1}{\sqrt{\text{No. of traces}}} \), i.e., there are no “ghost peaks” that might interfere with the retrieval of the correct key. Besides, the results are not limited to the first round of the first DES: the analysis equivalently works for other rounds of the first DES (to recover the remaining eight bit of \( k_{C,1} \)) and for the second DES iteration\(^7\) (to obtain \( k_{C,2} \)). In summary, as a result of this section, we conclude that the extraction of the complete secret 3DES key from a Mifare DESFire MF31CD40 can be carried out with approx. 250,000 traces, which can be collected in approx. seven hours using our current measurement setup.

\(^7\) in this case, alignment to the start pattern of this operation is necessary
6 Practical Attack: Template Attack on the Key Transfer

As observed during the profiling phase described in Sect. 4, the internal database of the DUT seems to be completely unprotected and exhibits a far stronger Hamming weight leakage than the cryptographic engine analyzed in Sect. 5. Thus, template attacks to obtain information on internal values transferred over this bus can be expected to work with a far lower number of traces compared to a CPA. Of special interest is the initialization of the cryptographic engine before the start of the actual 3DES operation: our analyses shows that the transfer of the secret key can be identified in the power trace of the DUT after the reader has sent the initial begin command in the authentication protocol (that is, during Step 1 in Fig. 3). Fig. 10a depicts a trace for the loading of the key and indicates

![Side-channel trace](image1.png)

(a) Side-channel trace

![Correlation](image2.png)

(b) Correlation

Fig. 10: Transfer of the 3DES key over the internal database

the internal order of operation: by repeatedly changing the key and performing a CPA using the Hamming weight of each key byte, we found out that the 3DES key is initialized in two steps. First, the upper eight byte \(k_{C:2}\) are transferred, starting with the least significant byte. After that, the lower half \(k_{C:1}\) (i.e., byte 0 ... 7) is transmitted, this time in reverse byte order. In both cases, the (redundant) parity bits are not removed prior to the key transfer, suggesting that they are discarded internally by the cryptographic engine. Fig. 10b exemplarily shows the corresponding correlation peaks for the key bytes 0 (blue), 7 (green), 8 (red) and 15 (cyan), allowing to exactly pinpoint the time instants at which information on a specific byte is leaking.

In contrast to CPA, template attacks require a profiling phase, i.e., a step during which the DUT is under full control of the adversary to estimate the statistical relation between the observable random variables — in our case the respective points in time of a trace — and the internal states that are to be distinguished (here, the value of a key byte). The resulting training set is then used to recover the desired values from a test set, i.e., traces for which the value of the key byte is considered unknown.

To systematically evaluate the success rate of template attacks for the case of the transfer of the key on the Mifare DESFire MF3iCD-40, we obtain 8,000
Algorithm 1 Template creation and matching procedure

\begin{algorithm}
\begin{algorithmic}
\FOR{$b = 0 \ldots 255$}
\STATE \{Estimate sample mean and covariance matrix from training set for byte $b$\}
\STATE $(\mu_b, \Sigma_b) \leftarrow \text{estimate} \left( S_b^{\text{training}} \right)$
\ENDFOR
\STATE \{Estimate average covariance matrix for the training data\}
\STATE $\Sigma = \frac{1}{255} \sum_{b=0}^{255} \Sigma_b$
\STATE \{Estimate sample mean and covariance matrix for the test data\}
\STATE $(\mu', \Sigma') \leftarrow \text{estimate} \left( S_b^{\text{test}} \right)$
\STATE \{Compute distance between the test and training data\}
\FOR{$b = 0 \ldots 255$}
\STATE $\delta_b \leftarrow \text{distance} \left( \mu_b, \Sigma_b, \Sigma', \mu' \right)$
\ENDFOR
\STATE \text{return} $\arg \min_b \delta_b$
\end{algorithmic}
\end{algorithm}

traces for each possible value of a targeted key byte\textsuperscript{8}. Here, we only address byte 0 and 15, however, our results hold for all other bytes as well. 4,000 traces are used for the training set, while the other 4,000 form the test set — in total, to cover all 256 possible values for a byte, we acquired $2 \cdot 256 \cdot 4,000 = 2,048,000$ traces. Again, we also compare the quality of analog demodulation compared to its digital equivalent and hence recorded traces both before and after the analog circuitry. Let $S_b^{\text{training}} = \{t_{b,0}, \ldots, t_{b,3999}\}$ be the training set and $S_b^{\text{test}} = \{t_{b,4000}, \ldots, t_{b,7999}\}$ the test set, where $t_{b,n}$ denotes the $n$th trace for a specific byte $0 \leq b < 256$, i.e., a $K \times 1$ vector of measured values. Given $S_b^{\text{test}}$ for a fixed but unknown key — in our case, the test set for some key byte value $b$ — the comparison to the training data is carried out as outlined in Alg. 1.

\text{estimate} (\cdot) is an algorithm that estimates the (pointwise) sample mean and covariance matrix from the respective set of traces, e.g., using the standard empirical formulae \cite{41}, distance (\cdot) is a suitable distance measure based on the previously estimated statistical parameters. The value for the key byte $b$ that minimizes the chosen distance measure is then returned as the most probable candidate for the given test traces. We exemplarily selected the following distance measures:

\textbf{Difference of means} The simplest case only evaluates the norm of the pointwise difference of the class means, i.e., \(\sum_{k=1}^K (\mu_k(k) - \mu'(k))^2\), discarding any information on the (co-)variances

\textbf{Euclidean} Assuming that the covariance matrix is diagonal, one obtains the Euclidean distance, \(\sum_{k=1}^K \frac{(\mu_k(k) - \mu'(k))^2}{\Sigma_k(k,k)}\), for which the differences are normalized using the pointwise variance

\textbf{Mahalanobis} Taking all available parameters of the distribution into account, the Mahalanobis distance \cite{22} is given as \((\mu_k(k) - \mu'(k))^T \Sigma^{-1} (\mu_k(k) - \mu'(k))\)

\textsuperscript{8} the training and test sets were acquired in separate measurement campaigns to rule out effects due to slightly varying environmental conditions
Table 1 summarizes the results of our template analysis both with (Table 1a) and without analog preprocessing (Table 1b). The average bit error rates were estimated by applying Alg. 1 for each byte, using the corresponding test set \( S_{test}^b \) and computing the Hamming distance between the detected and the actual value \( b \). Evidently, the upper half \( k_{C,2} \) can be recovered with significantly less error than \( k_{C,1} \), which interestingly admits a rather different leakage characteristic. In either case, the remaining uncertainty can be accounted for using exhaustive search over the key candidates, starting with the ones having the smallest distance to the training set.

<table>
<thead>
<tr>
<th>Keybyte</th>
<th>Distance</th>
<th>Bit error rate</th>
<th>Keybyte</th>
<th>Distance</th>
<th>Bit error rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>0 ((k_{C,1}))</td>
<td>DiffMeans 2.07</td>
<td></td>
<td>0 ((k_{C,1}))</td>
<td>DiffMeans 2.89</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Euclidean 2.14</td>
<td></td>
<td></td>
<td>Euclidean 2.66</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Mahalanobis 1.77</td>
<td></td>
<td></td>
<td>Mahalanobis 2.4</td>
<td></td>
</tr>
<tr>
<td>15 ((k_{C,2}))</td>
<td>DiffMeans 0.55</td>
<td></td>
<td>15 ((k_{C,2}))</td>
<td>DiffMeans 1.55</td>
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<tr>
<td></td>
<td>Euclidean 0.51</td>
<td></td>
<td></td>
<td>Euclidean 0.71</td>
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<tr>
<td></td>
<td>Mahalanobis 0.64</td>
<td></td>
<td></td>
<td>Mahalanobis 1.22</td>
<td></td>
</tr>
</tbody>
</table>

(a) With analog processing

(b) Without analog processing

Table 1: Average bit error rates for the key recovery based on templates using 4,000 traces

Limitations. Compared to the CPA presented in Sect. 5, the key recovery by means of templates might be carried out with far less traces and hence within a very short time\(^9\), thus potentially posing a severe security threat in a scenario in which an adversary either has to extract many different keys (e.g., due to a key distribution mechanism) or faces a constant risk of being detected. However, due to the necessity for a profiling phase, implementing the approach in practice turns out to be highly problematic: for the results given in Table 1, we could employ the same DUT, whereas in a real-world attack, the profiling and the attack device are different. In our experiments with different cards, we observed significantly differing leakage characteristics, even if the measurement setup (i.e., the positions of the EM probe and the DUT on the antenna) was kept exactly fixed. At present, we are therefore not able to apply the profiling data to a different card, however, we are currently evaluating calibration approaches and improved classifiers (e.g., using Principal Component Analysis (PCA) [35]). We were already able to obtain correct matchings at least for a subset of all possible key values.

\(^9\) in our current setup, recording 4,000 traces is a matter of minutes
7 Conclusion

We show several SCA attacks to fully recover the 3DES key of the Mifare DESFire MF31CD40, employing standard equipment in an academic measurement setup that can be built for approx. 3000 $. As we figured out the details of the implementation of the DUT, the attacks can be realized within a few hours (e.g., to collect approx. 250,000 traces for a CPA), and hence pose a severe threat to the security of DESFire-based real-world systems.

System integrators should be aware of the new security risks that arise from the presented attacks and can no longer rely on the mathematical security of the used 3DES cipher. Hence, in order to avoid, e.g., manipulation or cloning of smartcards used in payment or access control solutions, proper actions have to be taken: on the one hand, multi-level countermeasures in the backend allow to minimize the threat even if the underlying RFID platform is insecure, cf. [32]. For long-term security and when developing new systems, we recommend to use certified smartcards, for instance, the AES-based Mifare DESFire EV1, which passed an EAL-4+ evaluation [3] and which comprises SCA countermeasures that thwart the analysis methods presented in this paper.

Future Work Having demonstrated the fundamental susceptibility of the DESFire MF31CD40 towards SCA, there are several interesting directions for further research to consider: first, the SCA could be improved in order to work with a smaller number of traces, for instance, employing different alignment methods or model-independent side-channel distinguishers like Mutual Information Analysis (MIA) [11]. Apart from that, extensions of the proposed template attack may allow to reduce the error rate or to utilize the templates generated with a profiling device to recover the unknown key of another DESFire MF31CD40 card. Also, a combination of CPA and templates could further reduce the required number of traces. Finally, the developed techniques can be applied in order to attempt attacks on different cryptographic RFIDs, possibly including other (certified) high-security smartcards.

References

A Schematics

Fig. 11: Schematics of the analog full-wave rectifier circuit

Fig. 12: Schematics of the analog bandpass filter
B  Correlation Coefficient for Different Processing Methods

Fig. 13: Maximum correlation coefficient (32-bit Hamming distance $R_0 \rightarrow R_1$) for (a) analog demodulation (blue, solid), (b) digital demodulation (green, circle), (c) analog demodulation with DFA (red, square), (d) digital demodulation with DFA (cyan, diamond)